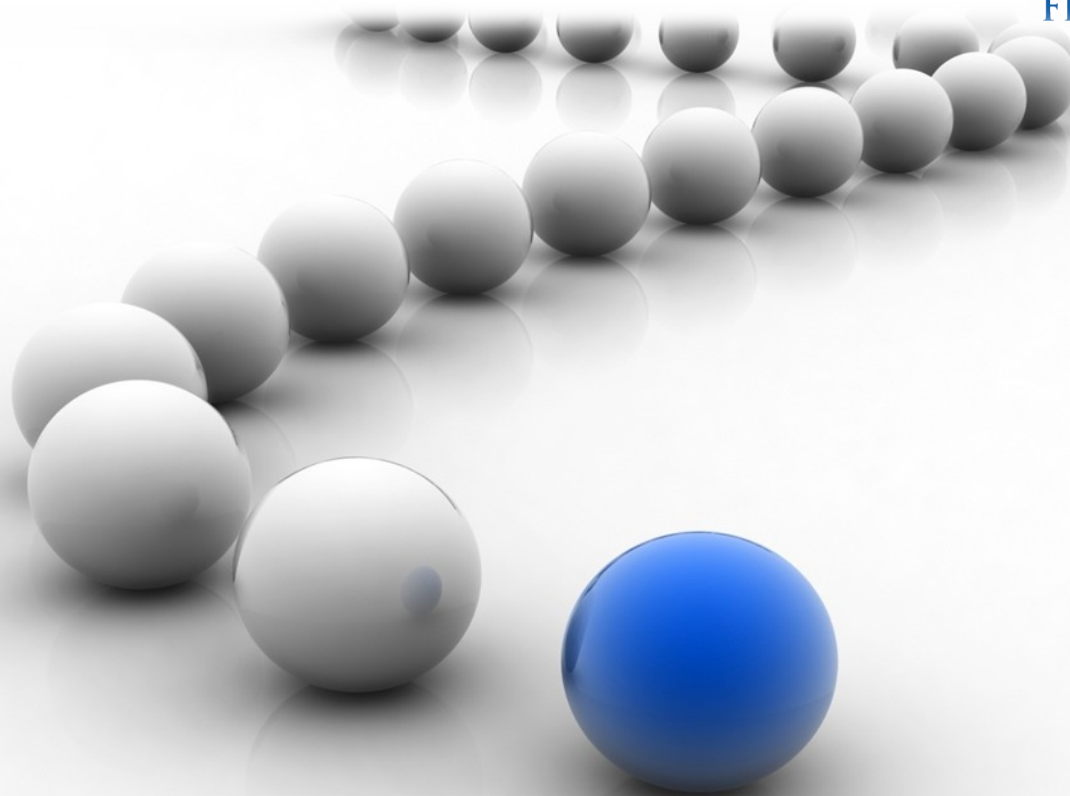


Do CDOs Work?



Jon Gregory

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Do CDOs Work?

Background

Economics of a CDO

Empirical test and examples

Conclusions

- In the period 1998 to 2007, CDOs increased exponentially in both volume and diversity
 - Prior to 2007, the CDO was seen as a successful financial innovation
- However, the global financial crisis was partly catalysed by an implosion in the CDO market and caused massive losses for:
 - Issuers (banks) through investments held, litigation, failed hedges, reputation
 - Investors, both in terms of default losses and those from forced liquidation
 - Third parties (e.g. rating agencies through loss of fees, reputation issues and litigation)
- An obvious question is therefore:
 - Is there something fundamentally wrong with the concept of a CDO?
 - Does it have economic value or is just a money making tool for investment bankers?

- This analysis will be based on a CDO under the following assumptions
 - Full capital structure (although this is not especially important)
 - Static portfolio (again particularly important as we care mainly about the initial portfolio)
 - Corporate credit risk (due to the richer data than for asset backed structures)
 - The ratings process used by ratings agencies for CDO structures during the period in question
- A CDO is broadly speaking
 - An investment at risk to a pre-defined range of losses on a certain portfolio
 - As such, the risk assessment requires an analysis of the multidimensional default distribution (which is quite complex)

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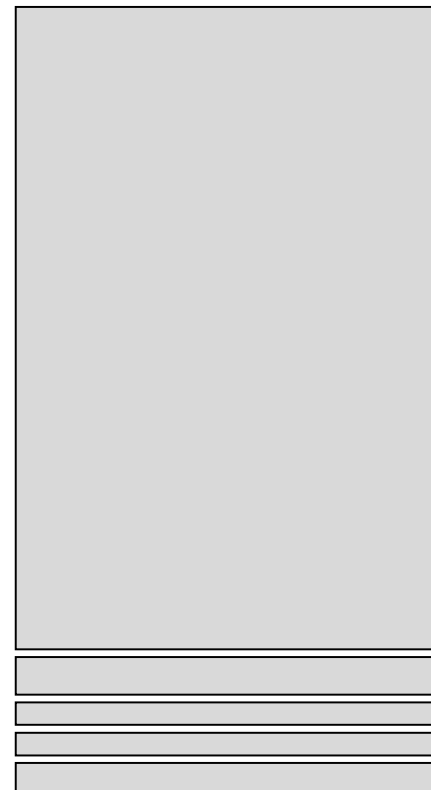
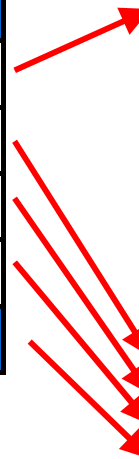
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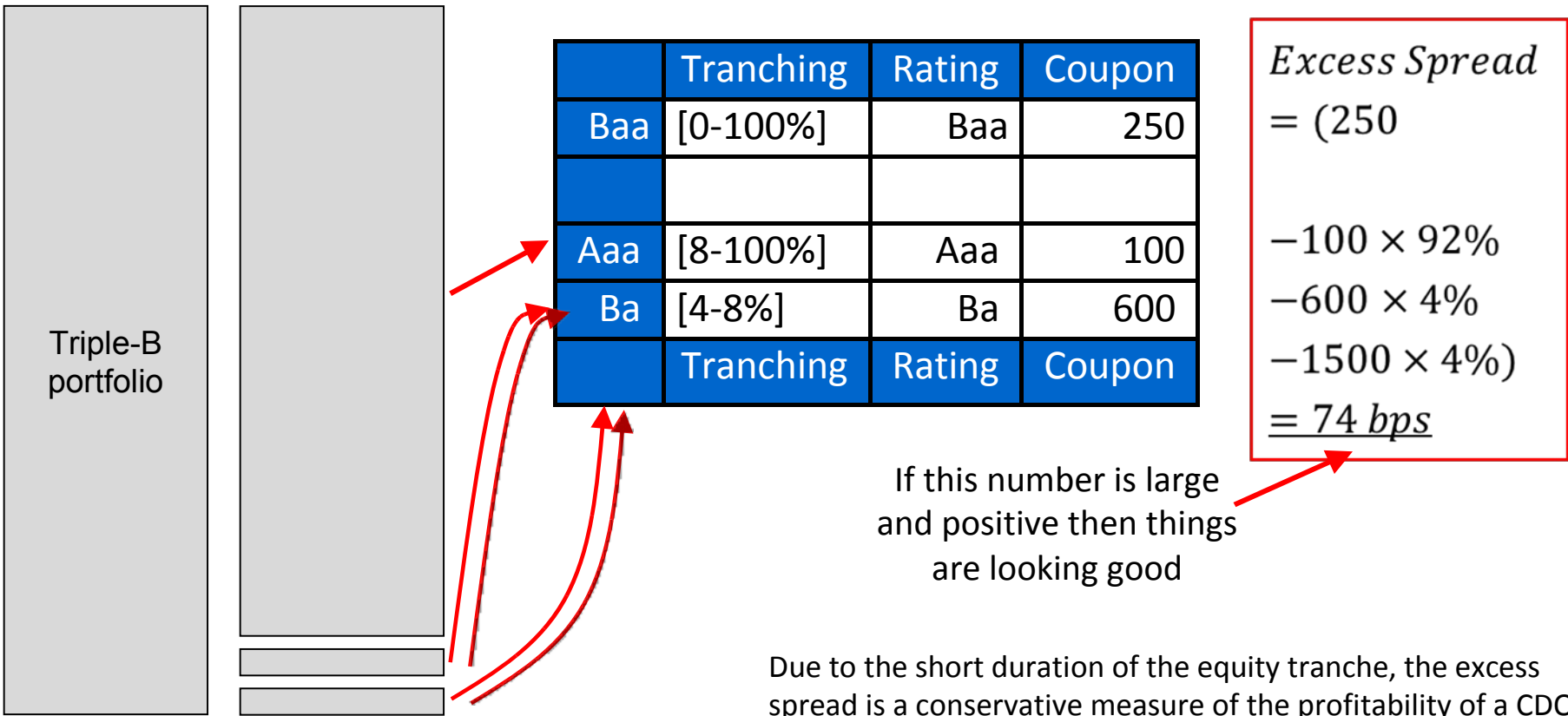
Example CDO

Class	Amount	Tranching	Rating	Funding
Super senior	850	[15-100%]	NR	Unfunded
Class A	50	[10-15%]	Aaa/AAA	Funded
Class B	30	[7-10%]	Aa2/AA	Funded
Class C	30	[4-7%]	Baa2/BBB	Funded
Class	Amount	Tranching	Rating	Funding



Example CDO Economics

- Very simple example (more rigorous one later)



- Suppose there is a continuum of underlying tranches (full capital structure)
 - Each tranche is denoted by i
 - The underlying portfolio is denoted by p
- Consider expected loss as the main quantitative characteristic of the tranche
 - Expected loss must be conserved across the structure

$$EL_P = \sum_i m_i EL_i$$

Expected loss for unit tranche
(under physical measure)

$$\sum_i m_i = 1$$

Tranche size

- **Investors will demand a premium for the losses they take**

- Let us represent this as a multiplier α which varies for the different tranches and original portfolio and therefore represents the risk aversion for a particular seniority
- Investors will be paid $\alpha_i m_i EL_i$
- The CDO will “work” if

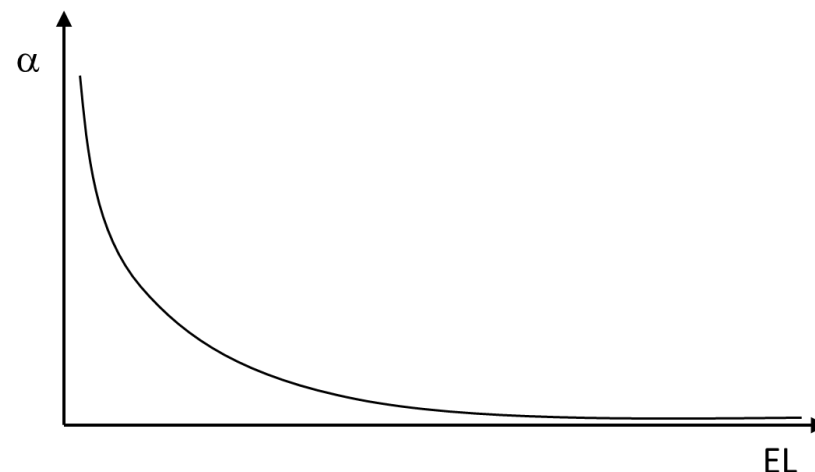
$$\alpha_p EL_P > \sum_i \alpha_i m_i EL_i$$

- This basically requires that it is possible to buy protection cheaper via the CDO tranches than it is on the underlying portfolio
- **Note that the α will be determined via the coupon demanded on the various tranches by investors**

- **How do we represent α ?**

- The primary consideration of investors was the rating of the underlying tranche
- In turn, the fundamental driver of ratings would be the expected loss of a tranche (or default probability in the case of Standard & Poor's)
- Hence we assume

$$\alpha_j = \left(\frac{a}{EL_j} \right)^b$$



- **Properties**

- Risk-neutral investors, $b = 0$
- Risk aversion for $a, b > 0$
- More relative risk aversion for small expected losses

- **What parameters are required for a CDO to work?**

- We require:

$$\alpha_p EL_p > \sum_i \alpha_i m_i EL_i \qquad \alpha_j = \left(\frac{a}{EL_j} \right)^b$$

- Which becomes:

$$\left(\frac{a}{EL_p} \right)^b EL_p > \sum_i \left(\frac{a}{EL_i} \right)^b m_i EL_i$$

- Simplifying to:

$$EL_p^{1-b} > \sum_i m_i EL_i^{1-b}$$

- Which is satisfied when $b < 1$

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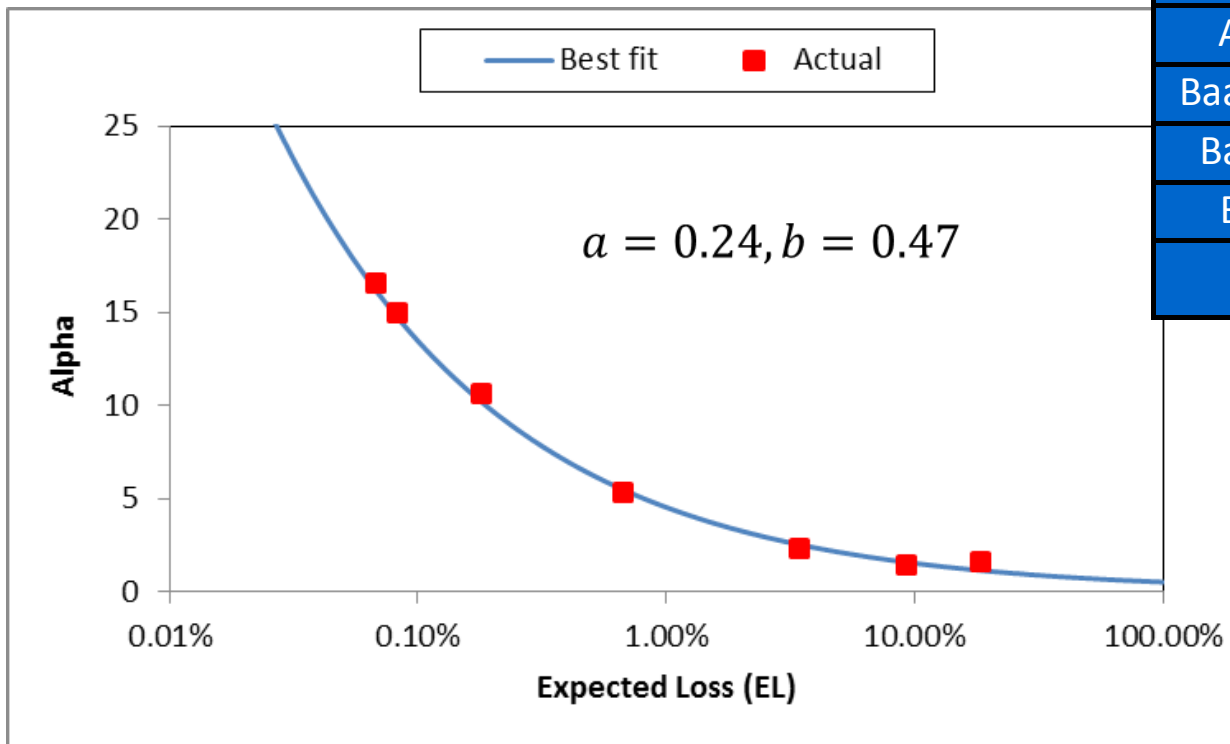
Empirical test and examples

Conclusions

- Hull, Predescu and White (2005)
 - Time period, December 1996 to July 2004
 - Merrill Lynch bond indices and Moody's data

	Default intensity		
	Real world	Risk-neutral	Ratio
Aaa	4	67	16.8
Aa	6	78	13.0
A	13	128	9.8
Baa	47	138	5.1
Ba	240	507	2.1
B	749	902	1.2
	Default intensity		

Assume recovery rate of 40%



Back to a simple example

- Rating assumptions

- Expected loss based
- Gaussian copula approach with flat correlation of 20%

Rating	Tranche	5-year exp loss	Multiplier	Protection value	Size	Spread (bps)
Baa	[0-100%]	1.296%	5.1	6.610%	100%	144
Aaa	[8-100%]	0.072%	16.8	1.210%	92%	26
Ba	[4-8%]	6.702%	2.1	14.074%	4%	321
Rating	Tranche	5-year exp loss	Multiplier	Protection value	Size	Spread (bps)

Excess Spread

= (144

– 26 × 92%

– 321 × 4%

– 1376 × 4%)

= 52 bps

Hamilton, D., P. Varma, S. Ou., and R. Cantor, "Default & Recovery Rates of Corporate Bond Issuers, A Statistical Review of Moody's Ratings Performance, 1920-2003", 2003, Moody's Investor Research, January.

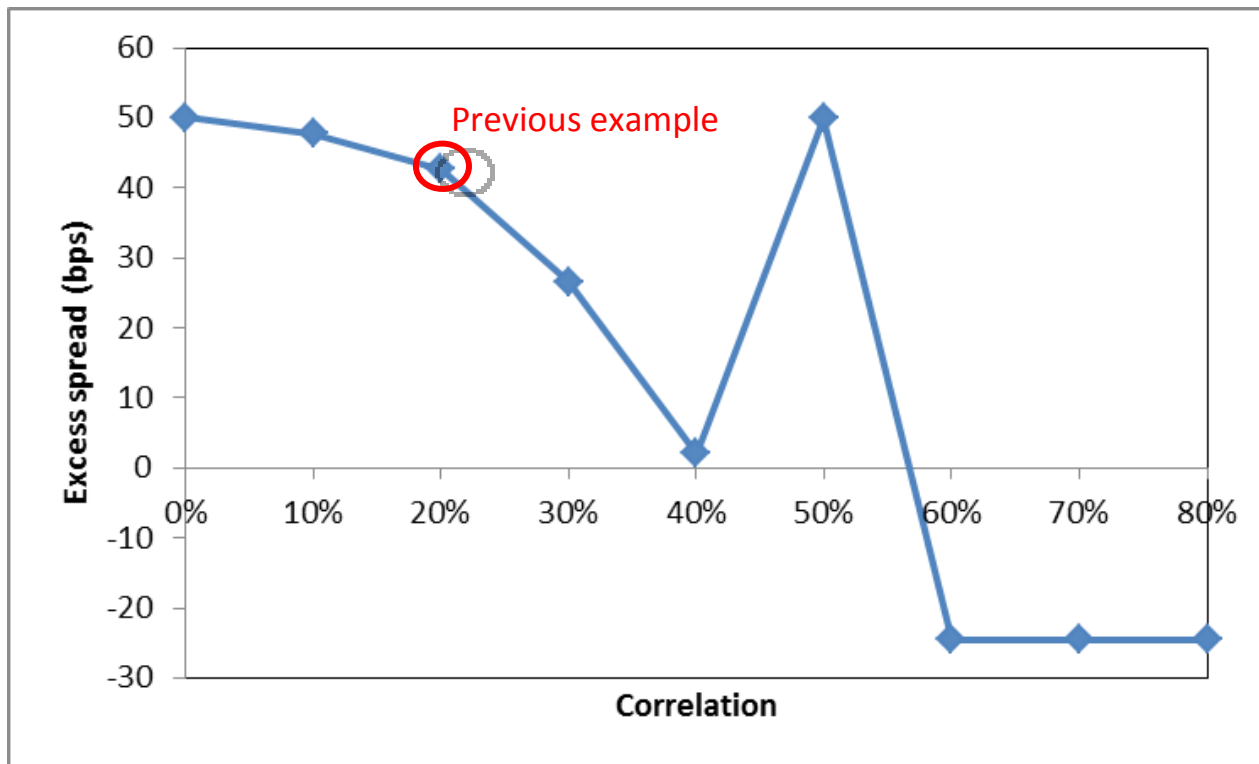
Hull, J., M. Predescu and A. White, 2005, "Bond Prices, Default Probabilities and Risk Premiums" Journal of Credit Risk, Vol. 1, No. 2, pp. 53-60.

Net protection value

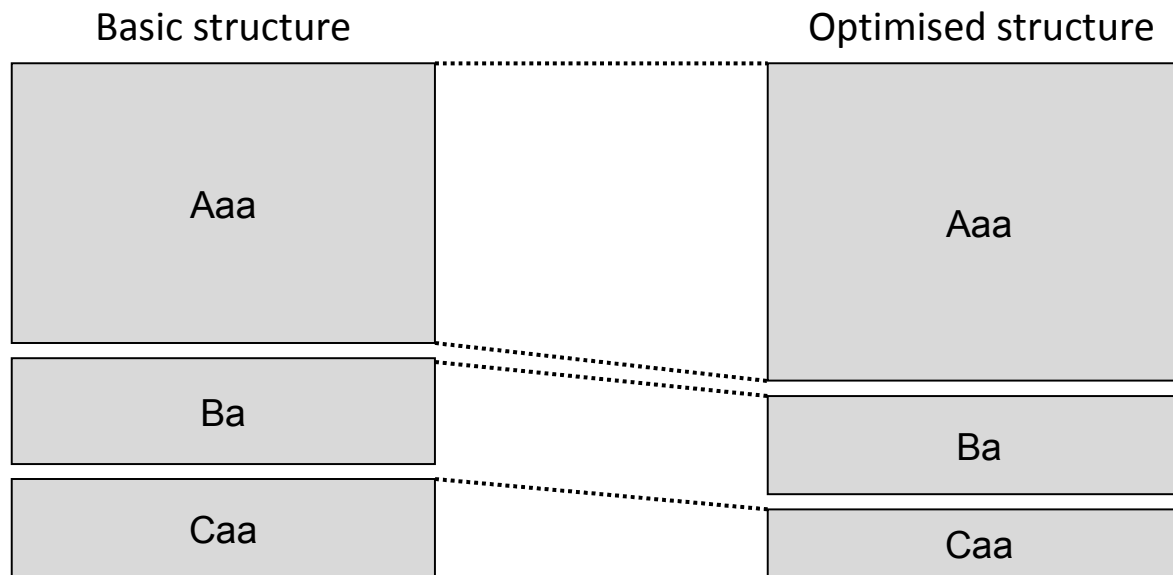
= 6.610% – 1.210% × 92% + 14.074% × 4% + 47.447% × 4% = 3.036%

- Assuming investors demand a return based on the expected loss (via the rating) of a tranche
 - A CDO always “works” due to the risk preferences of investors (the equity tranche is relatively cheap to get rid of due to the small alpha multiplier)
- Another implication of this is that rating agency modelling assumptions cannot cause the CDO to fail
 - For example, let us look at correlation assumptions

- Excess spread as a function of flat correlation assumptions in rating model
 - CDO clearly “fails” at high correlation



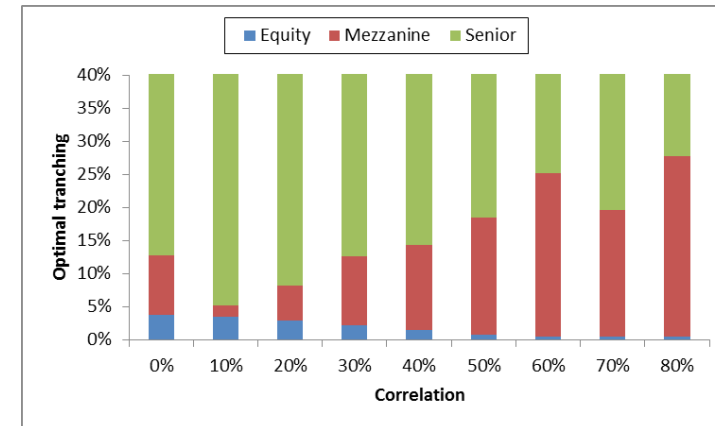
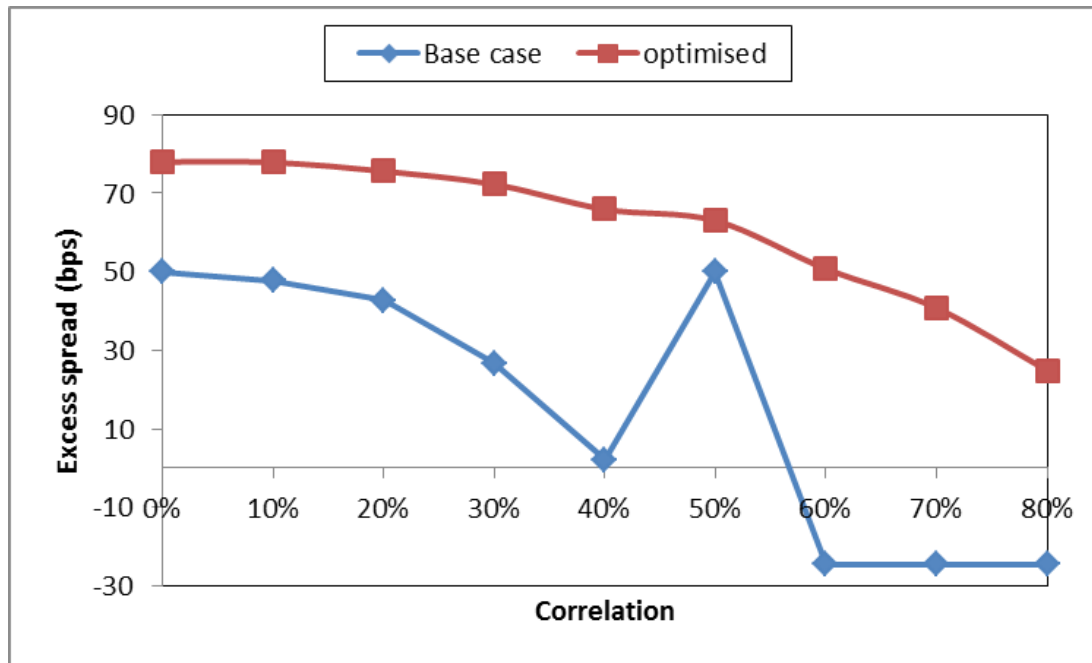
- Previous failure was due to the granularity in the ratings process



- Therefore we assume a simple optimisation
 - Make the equity tranche small enough to just support a given rating (Caa is best)
 - Find the size of the mezzanine tranche to give the best excess spread

Optimized structure (2)

- Now the CDO works at all correlation levels



- Note there is still some inherent granularity
 - Can't get any worse than Caa or better than Aaa

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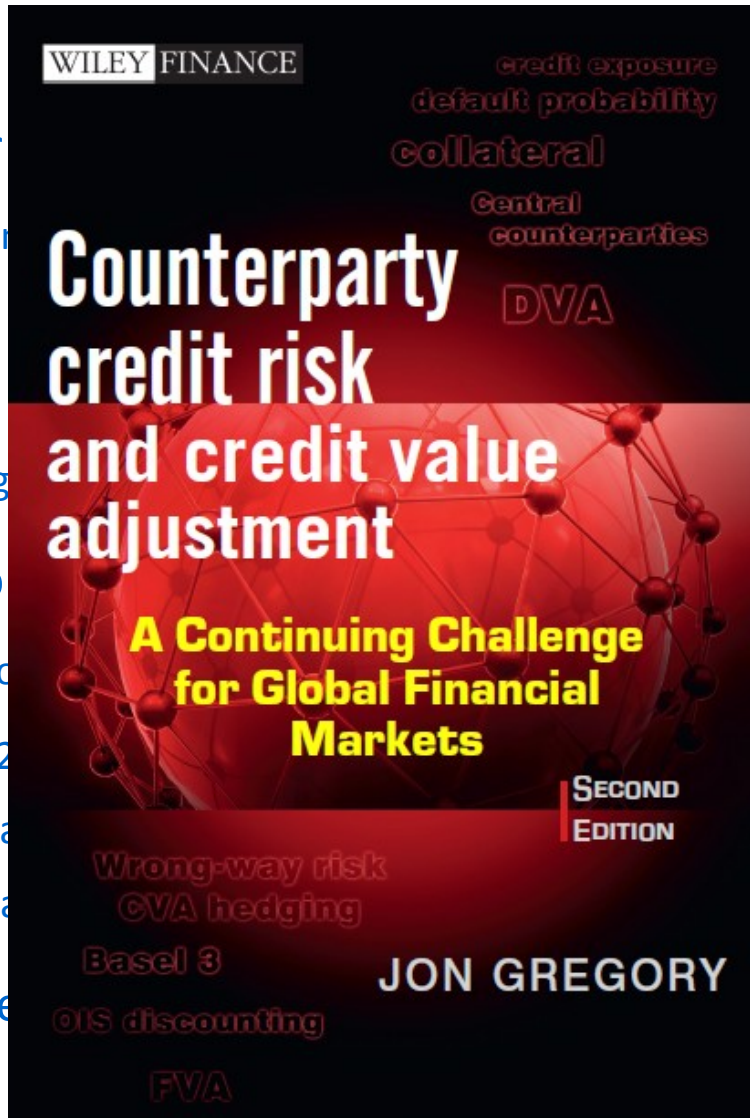
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Conclusions

- A CDO works due to
 - The risk preferences of investors
 - The expected loss methodology used in the ratings process
- A CDO is not a zero sum game
 - Both issuers and investors (and third parties) can gain
 - Just because an issuer makes money, no direct implication that investors are getting a bad deal
- Rating agencies were not at fault?
 - No modelling assumptions would have caused CDOs to be unprofitable
 - Although rating agencies primary reliance on quantitative models based on expected loss as the only metric could be seen as too simplistic and a fundamental flaw

So what did go wrong? (with CDOs at least)

- Lack of proper
– The more se
– Large senior
mitigate the
– E.g. see Greg
• Lack of ap
– Were investo
– Gibson, M., 2
Discussion Pa
“Economic ca
• Maybe the
problems



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