In this joint work with Andreas Hartmann, I will discuss necessary and sufficient conditions for every function in the range of a co-analytic Toeplitz operator, compressed to a model space, to have a finite non-tangential limit at a point on the unit circle. In a way, this result can be viewed as a generalization of a well-known result of Ahern and Clark which answers the same question when the co-analytic truncated Toeplitz operator is the identity operator on a model space.