Greedy Gray Codes and Pancake Flipping

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Abstract

The generation of combinatorial objects like permutations, necklaces, trees and graphs is a fundamental pursuit in \ldots Combinatorics! Given a set of objects, like all permutations given n, the goal is to develop an efficient algorithm to exhaustively list each permutation exactly once. If each successive permutation in the listing differs by a single operation (or a constant amount of change), we call the listing a *Gray code*. In this talk, we will discuss a surprisingly new way to look at Gray codes – from a Greedy perspective.

As an application, we consider a variation of the famous *Pancake Flipping Problem*, even when the pancakes are burnt on one side. In this problem, the goal is to iterate through all possible stacks of n different sized pancakes by only using a spatula and flipping part of the stack at each step. As an example, the following figure illustrates a listing of all pancake stacks for n = 5.



For all those interested in Graph Theory, we will consider an application on the pancake network (below) and discuss an open problem regarding spanning trees.

