A Model for Solar RenewableEnergy Certificates:Shining some light on price dynamicsand optimal market design

Michael Coulon

(work at Princeton University with Javad Khazaei & Warren Powell)

August 15th, 2013

Workshop on Electricity, Energy and Commodities Risk Management

Field's Institute, Toronto, Canada

M.Coulon@sussex.ac.uk

University of Sussex

Carbon Market Outlook

Outlook for EU market bleak right now... *(Apr 2013 Economist article)*

ETS, RIP?

The failure to reform Europe's carbon market will reverberate round the world Apr 20th 2013 | From the print edition

On the other hand, other regions are developing (eg, California, China).

Toronto, Aug 15th 2013 – p.2/27

In the US, about 30 states recently introduced ^a Renewable Portfolio Standard(RPS). About 10 have set up markets for tradeable certificates called SRECs(or more generally RECs) to achieve these RPS targets.

(map taken from: US DoE-NREL repor^t by Bird, Heeter, Kreycik, 2011)

While cap-and-trade markets have struggled in recently (low prices, politicalstalemates, etc.), ^a new environmental market is growing. How does it work?

•Government sets increasing requirements on $%$ solar power in the generation mix each future year. (ie, set $R^{(1)}, R^{(2)}, \ldots$ for yrs 1, 2,..)

- •Government sets increasing requirements on $%$ solar power in the generation mix each future year. (ie, set $R^{(1)}, R^{(2)}, \ldots$ for yrs 1, 2,..)
- • Solar generators are issued SRECs (solar renewable energy certificates)for each MWh of power generated and can sell these in the market.

- •Government sets increasing requirements on $%$ solar power in the generation mix each future year. (ie, set $R^{(1)}, R^{(2)}, \ldots$ for yrs 1, 2,..)
- • Solar generators are issued SRECs (solar renewable energy certificates)for each MWh of power generated and can sell these in the market.
- • All 'load serving entities' (utilities) must submit sufficient SRECs eachyear to meet requirement, or else pay a penalty (say, $\pi^{(1)}, \pi^{(2)}, \ldots$).

- •Government sets increasing requirements on $%$ solar power in the generation mix each future year. (ie, set $R^{(1)}, R^{(2)}, \ldots$ for yrs 1, 2,..)
- • Solar generators are issued SRECs (solar renewable energy certificates)for each MWh of power generated and can sell these in the market.
- • All 'load serving entities' (utilities) must submit sufficient SRECs eachyear to meet requirement, or else pay a penalty (say, $\pi^{(1)}, \pi^{(2)}, \ldots$).
- \bullet SRECs have ^a 'vintage year' but can typically be banked for several future years. (currently 5 year life in NJ, so 4 banking chances).

While cap-and-trade markets have struggled in recently (low prices, politicalstalemates, etc.), ^a new environmental market is growing. How does it work?

- •Government sets increasing requirements on $%$ solar power in the generation mix each future year. (ie, set $R^{(1)}, R^{(2)}, \ldots$ for yrs 1, 2,..)
- • Solar generators are issued SRECs (solar renewable energy certificates)for each MWh of power generated and can sell these in the market.
- • All 'load serving entities' (utilities) must submit sufficient SRECs eachyear to meet requirement, or else pay a penalty (say, $\pi^{(1)}, \pi^{(2)}, \ldots$).
- \bullet SRECs have ^a 'vintage year' but can typically be banked for several future years. (currently 5 year life in NJ, so 4 banking chances).

A market-based alternative to direct subsidies for clean technologies!

While cap-and-trade markets have struggled in recently (low prices, politicalstalemates, etc.), ^a new environmental market is growing. How does it work?

- •Government sets increasing requirements on $%$ solar power in the generation mix each future year. (ie, set $R^{(1)}, R^{(2)}, \ldots$ for yrs 1, 2,..)
- • Solar generators are issued SRECs (solar renewable energy certificates)for each MWh of power generated and can sell these in the market.
- All 'load serving entities' (utilities) must submit sufficient SRECs each year to meet requirement, or else pay a penalty (say, $\pi^{(1)}, \pi^{(2)}, \ldots$).
- \bullet SRECs have ^a 'vintage year' but can typically be banked for several future years. (currently 5 year life in NJ, so 4 banking chances).

A market-based alternative to direct subsidies for clean technologies!But... if prices are too volatile, it can be very risky for solar investors relying on revenues from selling SRECs, counteracting the goal of the market

 \implies Market design very important!

The New Jersey SREC market is the biggest in the US (among about 10states; similar markets for 'green certificates' also exist in Europe and Asia)

- •Most ambitious target of over 4% solar energy by 2028.
- •Highest recorded prices so far at about \$700 per SREC.
- • Rapid growth witnessed in solar installations in recent years. (plot below from NJ Clean Energy)

The rules of the NJ market have been changed many times. Just ^a summary:

What about historical prices? Very high (near π) until very recently...

Historical (monthly) issuance data easily available online. Solar generation isgrowing fast (faster than R), with clear seasonality... will the trend continue?

Stochastic models for SREC prices

How can we model an SREC price p_t^y (for vintage year $y \in \mathbb{N}$)?

- •Essentially no literature (useful reports, websites, but not price models!)
- • Instead we draw on strong parallels with carbon emissions markets(with supply and demand reversed... here governmen^t fixes *demand*)

Stochastic models for SREC prices

How can we model an SREC price p_t^y (for vintage year $y \in \mathbb{N}$)?

- •Essentially no literature (useful reports, websites, but not price models!)
- • Instead we draw on strong parallels with carbon emissions markets(with supply and demand reversed... here governmen^t fixes *demand*)

Consider a single-year case $t \in [y]$ − $[1, y]$ (no banking). Like carbon,

- •• SRECs are traded financial contracts, and thus martingales under $\mathbb Q$
- •• At the compliance date, they should be worth either 0 or the penalty π_t^y

Stochastic models for SREC prices

How can we model an SREC price p_t^y (for vintage year $y \in \mathbb{N}$)?

- •Essentially no literature (useful reports, websites, but not price models!)
- • Instead we draw on strong parallels with carbon emissions markets(with supply and demand reversed... here governmen^t fixes *demand*)

Consider a single-year case $t \in [y]$ − $[1, y]$ (no banking). Like carbon,

- •• SRECs are traded financial contracts, and thus martingales under $\mathbb Q$
- •• At the compliance date, they should be worth either 0 or the penalty π_t^y Therefore, for $t\in[y]$ $1,y],$

$$
p_t^y = e^{-r(y-t)} \pi_t^y \mathbb{E}_t \left[1_{\{ \int_{y-1}^y g_u du < R_t^y \}} \right],
$$

= $e^{-r(y-t)} \pi_t^y \mathbb{P} \left\{ \int_t^y g_u du < R_t^y - \int_{y-1}^t g_u du \right\},$

where g_t is the annualized solar generation rate (ie, SREC issuance rate).

Next step: Include k years of banking, such that a vintage year y SREC is valid for compliance at times

$$
t\in\{y,y+1,\ldots,y+k\}
$$

Then the price today is ^a max over all future shortage probabilities:

$$
p_t^y = \max_{v \in \{\lceil t \rceil, \lceil t \rceil + 1, \dots, y + k\}} e^{-r(v-t)} \pi_t^v \mathbb{E}_t \left[1_{\{b_v = 0\}} \right]
$$

where b_t is the accumulated SREC supply (this year's plus banked):

$$
b_t = \begin{cases} \max\left(0, b_{t-1} + \int_{t-1}^t g_u \mathrm{d}u - R_t^t\right) & t \in \mathbb{N}, \\ b_{\lceil t \rceil - 1} + \int_{\lceil t \rceil - 1}^t g_u \mathrm{d}u & t \notin \mathbb{N}. \end{cases}
$$

(Note that at $t \in \mathbb{N}$, $b_t = 0$ if the requirement is not met.)

Next step: Include k years of banking, such that a vintage year y SREC is valid for compliance at times

$$
t\in\{y,y+1,\ldots,y+k\}
$$

Then the price today is ^a max over all future shortage probabilities:

$$
p_t^y = \max_{v \in \{\lceil t \rceil, \lceil t \rceil + 1, \dots, y + k\}} e^{-r(v-t)} \pi_t^v \mathbb{E}_t \left[1_{\{b_v = 0\}} \right]
$$

where b_t is the accumulated SREC supply (this year's plus banked):

$$
b_t = \begin{cases} \max\left(0, b_{t-1} + \int_{t-1}^t g_u \mathrm{d}u - R_t^t\right) & t \in \mathbb{N}, \\ b_{\lceil t \rceil - 1} + \int_{\lceil t \rceil - 1}^t g_u \mathrm{d}u & t \notin \mathbb{N}. \end{cases}
$$

(Note that at $t \in \mathbb{N}$, $b_t = 0$ if the requirement is not met.)

Final step: A stochastic model for solar generation rate g_t ?

NJ SREC issuance data

Log plot of total monthly issuance shows some noise but also ^a clear trend (slope $= 0.64$) and seasonality:

Like for electricity demand, perhaps model g_t with an OU process plus ^a trend and cosines? Anything missing?

Toronto, Aug 15th 2013 – p.11/27

Yes, **feedback** of SREC prices on generation growth is crucial!

Yes, **feedback** of SREC prices on generation growth is crucial!

 \bullet • We first fit seasonality and Gaussian noise term ε_t :

 $g_t = \hat{g}_t(p) \exp(a_1 \sin(4\pi t) + a_2 \cos(4\pi t) + a_3 \sin(2\pi t) + a_4 \cos(2\pi t) + \varepsilon_t),$

Yes, **feedback** of SREC prices on generation growth is crucial!

• We first fit seasonality and Gaussian noise term ε_t :

 $g_t = \hat{g}_t(p) \exp(a_1 \sin(4\pi t) + a_2 \cos(4\pi t) + a_3 \sin(2\pi t) + a_4 \cos(2\pi t) + \varepsilon_t),$

•• We then assume that the average annual generation rate \hat{g}_t grows as:

$$
\frac{\ln(\hat{g}_{t+\Delta t}) - \ln(\hat{g}_t)}{\Delta t} = a_5 + a_6 \bar{p}_t, \quad \text{for } a_5 \in \mathbb{R}, a_6 > 0,
$$

where a_6 captures sensitivity to prices (degree of feedback).

Yes, **feedback** of SREC prices on generation growth is crucial!

• We first fit seasonality and Gaussian noise term ε_t :

 $g_t = \hat{g}_t(p) \exp(a_1 \sin(4\pi t) + a_2 \cos(4\pi t) + a_3 \sin(2\pi t) + a_4 \cos(2\pi t) + \varepsilon_t),$

•• We then assume that the average annual generation rate \hat{g}_t grows as:

$$
\frac{\ln(\hat{g}_{t+\Delta t}) - \ln(\hat{g}_t)}{\Delta t} = a_5 + a_6 \bar{p}_t, \quad \text{for } a_5 \in \mathbb{R}, a_6 > 0,
$$

where a_6 captures sensitivity to prices (degree of feedback).

• \bar{p}_t allows for dependence on historical average prices, not just today's:

$$
\bar{p}_t^y = \delta p_t^y + (1 - \delta)\bar{p}_{t-\Delta t}^y \quad \text{and} \quad \bar{p}_0^y = p_0^y
$$

Yes, **feedback** of SREC prices on generation growth is crucial!

• We first fit seasonality and Gaussian noise term ε_t :

 $g_t = \hat{g}_t(p) \exp(a_1 \sin(4\pi t) + a_2 \cos(4\pi t) + a_3 \sin(2\pi t) + a_4 \cos(2\pi t) + \varepsilon_t),$

•• We then assume that the average annual generation rate \hat{g}_t grows as:

$$
\frac{\ln(\hat{g}_{t+\Delta t}) - \ln(\hat{g}_t)}{\Delta t} = a_5 + a_6 \bar{p}_t, \quad \text{for } a_5 \in \mathbb{R}, a_6 > 0,
$$

where a_6 captures sensitivity to prices (degree of feedback).

• \bar{p}_t allows for dependence on historical average prices, not just today's:

$$
\bar{p}_t^y = \delta p_t^y + (1 - \delta)\bar{p}_{t-\Delta t}^y \quad \text{and} \quad \bar{p}_0^y = p_0^y
$$

This completes the model. We can now solve by dynamic programming. (Between years $p_t^y=e^{-r}$ $\Delta t \mathop{\mathbb{E}}_{\mathbf{L}}^{\mathbb{Q}}$ $\int_t^{\mathbb{Q}}[p_{t+\Delta t}^y],$ while jumps can occur at $t\in\mathbb{N}.$)

Summary of the Algorithm

Recall: Firstly the price today as ^a maximum over expected payoffs:

$$
p_t^y = \max_{v \in \{\lceil t \rceil, \lceil t \rceil + 1, \dots, y + k\}} e^{-r(v-t)} \pi_t^v \mathbb{E}_t \left[1_{\{b_v = 0\}} \right].
$$

Discretize and initialize $p_T^y(b_T, \hat{g}_T)$ $(T) = 1_{\{b_T = 0\}}$ at $T = y + k$. Then:

Summary of the Algorithm

Recall: Firstly the price today as ^a maximum over expected payoffs:

$$
p_t^y = \max_{v \in \{\lceil t \rceil, \lceil t \rceil + 1, \dots, y + k\}} e^{-r(v-t)} \pi_t^v \mathbb{E}_t \left[1_{\{b_v = 0\}} \right].
$$

Discretize and initialize $p_T^y(b_T, \hat{g}_T)$ $(T) = 1_{\{b_T = 0\}}$ at $T = y + k$. Then:

• For $t \notin \mathbb{N}$, solve $p_t^y = e^$ $r\,$ $\Delta t \mathop{\mathbb{E}}_{\mathbf{L}}^{\mathbb{Q}}$ $\int_t^{\mathbb{Q}}[p_{t+\Delta t}^y],$ a fixed point problem with

$$
p_t^y \uparrow \Longrightarrow \hat{g}_{t+\Delta t} \uparrow \Longrightarrow b_{t+\Delta t} \uparrow \Longrightarrow \text{RHS} \downarrow.
$$

• For
$$
t \in \mathbb{N}
$$
, solve $p_t^y = \max\left(\pi_t^t 1_{\{b_t = 0\}}, e^{-r\Delta t} \mathbb{E}_t^{\mathbb{Q}}[p_{t+\Delta t}^y]\right)$

Summary of the Algorithm

Recall: Firstly the price today as ^a maximum over expected payoffs:

$$
p_t^y = \max_{v \in \{\lceil t \rceil, \lceil t \rceil + 1, \dots, y + k\}} e^{-r(v-t)} \pi_t^v \mathbb{E}_t \left[1_{\{b_v = 0\}} \right].
$$

Discretize and initialize $p_T^y(b_T, \hat{g}_T)$ $(T) = 1_{\{b_T = 0\}}$ at $T = y + k$. Then:

• For $t \notin \mathbb{N}$, solve $p_t^y = e^$ $r\,$ ∆ $^t\mathbb{E}^\mathbb{Q}_+$ $\int_t^{\mathbb{Q}}[p_{t+\Delta t}^y],$ a fixed point problem with

$$
p_t^y \uparrow \implies \hat{g}_{t+\Delta t} \uparrow \implies b_{t+\Delta t} \uparrow \implies \text{RHS} \downarrow.
$$

• For
$$
t \in \mathbb{N}
$$
, solve $p_t^y = \max\left(\pi_t^t 1_{\{b_t = 0\}}, e^{-r\Delta t} \mathbb{E}_t^{\mathbb{Q}}[p_{t + \Delta t}^y]\right)$

Analogously for carbon (emissions E_t , allowance price A_t), the FBSDE:

$$
dE_t = \mu_E(A_t, \cdot)dt, \qquad E_0 = 0,
$$

$$
dA_t = rA_t dt + Z_t dW_t \qquad A_T = \pi 1_{\{E_T \ge \kappa\}},
$$

where the emissions drift $\mu_E(A_t, \cdot)$ is decreasing in A_t .

Solving algorithm produces a surface $P_t(b_t, \hat{g}_t)$ for each time. For 2013 SRECs near the end of the first year:

Same price surface but six months later:

As with carbon, price surface 'diffuses' from its digital option shape at eachcompliance date (but not exactly ^a digital payoff if banking provides value):

Toronto, Aug 15th 2013 – p.16/27

Sensitivity to feedback parameter a_6 :

Comparison to history

After fitting parameters, we compare historical market vs model prices:

- •Overall price behaviour through history reasonably encouraging
- •Also, provides some evidence about the level of feedback in the market

Comparison to history

Price elasticity parameter set to $a_6 = 7 \times 10^{-4}$ throughout, except:

- •• For 2013A line, $a_6 = 5 \times 10^{-4}$ (low feedback)
- \bullet • For 2013B line, $a_6 = 1 \times 10^{-3}$ (high feedback)

Toronto, Aug 15th 2013 – p.19/27

Policy Analysis

SREC markets (just like cap-and-trade) are very sensitive to market design. For example, choosing an appropriate requirement growth schedule:

Policy Analysis

A larger number of banking years clearly produces greater price stability:

Policy Analysis - Other Ideas?

Inherent instability (in both REC and carbon markets) is due to the digital payoff functions... why not try something smoother? (eg, the blue line below)

A sloped penalty function implies:

- •^A non-trivial (model-dependent) banking decision each year
- •^A resulting threshold analogous to Am. options' 'exercise boundary'

Simulated paths reveal greater stability:

Long-term simulations of different vintages reveal that with ^a sloped(graduated) penalty policy:

- •Lower volatility, more stable prices, fewer sudden price drops
- •Much smaller price gaps between different vintage years

Long-term simulations of different vintages reveal that with ^a sloped(graduated) penalty policy:

- •Lower volatility, more stable prices, fewer sudden price drops
- •Much smaller price gaps between different vintage years

Simulations above use the same set of random numbers but for the step case $(\Delta = 0)$ on the left and slope case ($\Delta = 500$ GWh) on the right.

Mean of simulations reveals similar patterns (again $\Delta = 0$ on left, $\Delta = 500$ GWh on right)

Note: Why do the annual drops in mean price not clash with 'no arbitrage'?

- • Expectation is taken over all paths, including those for which bankingis not optimal (ie, SRECs should all be used up for compliance)
- •Hence no price drops in practice as that vintage would disappear.

Mean of simulations reveals similar patterns (again $\Delta = 0$ on left, $\Delta = 500$ GWh on right)

Note: Why do the annual drops in mean price not clash with 'no arbitrage'?

- • Expectation is taken over all paths, including those for which bankingis not optimal (ie, SRECs should all be used up for compliance)
- •Hence no price drops in practice as that vintage would disappear.

While useful for smoothing dynamics, changing the penalty alone does notaddress long-term supply and demand imbalances which have often triggernew legislation. Any other way?

While useful for smoothing dynamics, changing the penalty alone does notaddress long-term supply and demand imbalances which have often triggernew legislation. Any other way?

• ^A dynamically adaptive requirement level each year. For example, set

$$
\tilde{R}^y = R^y + \lambda \left(b_{y-1-\epsilon} - R^{y-1} \right), \qquad \lambda \in (0,1).
$$

While useful for smoothing dynamics, changing the penalty alone does notaddress long-term supply and demand imbalances which have often triggernew legislation. Any other way?

• ^A dynamically adaptive requirement level each year. For example, set

$$
\tilde{R}^y = R^y + \lambda \left(b_{y-1-\epsilon} - R^{y-1} \right), \qquad \lambda \in (0,1).
$$

•• Policy could work in conjunction with a function $\pi(R)$ for adaptive penalties which gradually reduce as long-term solar targets approach.

While useful for smoothing dynamics, changing the penalty alone does notaddress long-term supply and demand imbalances which have often triggernew legislation. Any other way?

• ^A dynamically adaptive requirement level each year. For example, set

$$
\tilde{R}^y = R^y + \lambda \left(b_{y-1-\epsilon} - R^{y-1} \right), \qquad \lambda \in (0,1).
$$

- •• Policy could work in conjunction with a function $\pi(R)$ for adaptive penalties which gradually reduce as long-term solar targets approach.
- •Unrealistically complicated? Currently in Massachusetts, they use:

Total Compliance Obligation 2013 ⁼ Total Compliance Obligation 2012+[Total SRECs Generated (projected) 2012 - SRECs Generated (actual) 2011] x 1.3 $\,$ *⁺ Banked Volume 2011 ⁺ Auction Volume 2011 - ACP Volume 2011*

While useful for smoothing dynamics, changing the penalty alone does notaddress long-term supply and demand imbalances which have often triggernew legislation. Any other way?

• ^A dynamically adaptive requirement level each year. For example, set

$$
\tilde{R}^y = R^y + \lambda \left(b_{y-1-\epsilon} - R^{y-1} \right), \qquad \lambda \in (0,1).
$$

- •• Policy could work in conjunction with a function $\pi(R)$ for adaptive penalties which gradually reduce as long-term solar targets approach.
- •Unrealistically complicated? Currently in Massachusetts, they use:

Total Compliance Obligation 2013 ⁼ Total Compliance Obligation 2012+[Total SRECs Generated (projected) 2012 - SRECs Generated (actual) 2011] x 1.3 $\,$ *⁺ Banked Volume 2011 ⁺ Auction Volume 2011 - ACP Volume 2011*

•• Finally, in addition to this formula for R , Mass implements a \$300 fixed-price auction each year, as ^a form of 'price floor mechanism'.

Stabilizing prices (to encourage more investment) without defeating the point of the market is really striking ^a balance between price and quantity targets. Insummary, what design tools can regulators consider?

• Continue to stretch the banking life of SRECs

- •Continue to stretch the banking life of SRECs
- • Change the digital payoff in the implementation of the penalty tosomething smoother? (slope instead of step)

- Continue to stretch the banking life of SRECs
- • Change the digital payoff in the implementation of the penalty tosomething smoother? (slope instead of step)
- Allow next year's requirement to adapt / respond to this year's surplus / shortage? (tried by Massachusetts already)

- Continue to stretch the banking life of SRECs
- • Change the digital payoff in the implementation of the penalty tosomething smoother? (slope instead of step)
- Allow next year's requirement to adapt / respond to this year's surplus / shortage? (tried by Massachusetts already)
- Allow next year's penalty to adapt / respond to this year's prices? (tried by Pennsylvania already)

- Continue to stretch the banking life of SRECs
- • Change the digital payoff in the implementation of the penalty tosomething smoother? (slope instead of step)
- Allow next year's requirement to adapt / respond to this year's surplus / shortage? (tried by Massachusetts already)
- Allow next year's penalty to adapt / respond to this year's prices? (tried by Pennsylvania already)
- • Establish an organization to periodically reassess requirement? (likecentral banks for money supply!)

Stabilizing prices (to encourage more investment) without defeating the point of the market is really striking ^a balance between price and quantity targets. Insummary, what design tools can regulators consider?

- Continue to stretch the banking life of SRECs
- • Change the digital payoff in the implementation of the penalty tosomething smoother? (slope instead of step)
- Allow next year's requirement to adapt / respond to this year's surplus / shortage? (tried by Massachusetts already)
- Allow next year's penalty to adapt / respond to this year's prices? (tried by Pennsylvania already)
- • Establish an organization to periodically reassess requirement? (likecentral banks for money supply!)

Some promising ideas, but details are tricky and more work on understanding and modeling the resulting price dynamics is crucial!